# Georgia Institute of Technology Daniel Guggenheim School of Aerospace Engineering

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## AE 6580: Aerospace Nonlinear Control

### Topics:

Dynamical Systems and Differential Equations

- System Equilibria
- Nonlinear Differential Equations
- Dynamical Systems, Flows, and Vector Fields
- Existence and Uniqueness of Solutions
- Continuous Dependence on System Initial Conditions and Parameters
- Continuity, Uniform Continuity, and Lipschitz Continuity
- Limit Points, Limit Sets, and Attractors

Nonlinear Second-Order Dynamical Systems

- Vector Fields, Flows, Phase Portraits
- Nodes, Saddles, Foci, and Centers
- Isocline Method and Linearization
- Periodic Orbits and Limit Cycles
- Poincare, Bendixon, and Poincare-Bendixon Theorems

Stability Theory for Nonlinear Dynamical Systems

- Lyapunov Stability, Asymptotic Stability, Exponential Stability
- Lyapunov Stability Theorems
- Lyapunov Function Constructions
- Krasovskii's Method, Variable Gradient Method, Zubov's Method
- Stability of Linear Systems and Lyapunov's Linearization Method
- Invariance Principal
- Invariant Set Stability Theorems
- Converse Lyapunov Theorems
- Instability Theorems
- Partial Stability
- Stability Theory for Time-Varying Systems
- Lagrange Stability, Boundedness, and Ultimate Boundedness
- Poincare Maps and Stability of Periodic Orbits

Dissipativity Theory for Nonlinear Dynamical Systems

- Dissipativity and Exponential Dissipativity
- Lagrangian and Hamiltonian Dynamical Systems
- Passivity and Nonexpansivity
- Storage Functions, Supply Rates, Available Storage, Required Supply
- Kalman-Yakvbovich-Popov Conditions

• Positive Real and Bounded Real Dynamical Systems

Absolute Stability Theory

- The Lure Problem
- Positivity Theorem, Circle Theorem, Popov Theorem
- Stability of Feedback Intercorrections
- Small Gain and Positivity Theorems
- Connections to Robust Control

Input-Output Stability

- Lp Spaces and Extended Lp Spaces
- Causality
- Lp Stability and the Small Gain Theorem
- Connections to Nonexpansivity
- Input-to-State Stability
- Applications to Linear Systems

#### Nonlinear Control

- Energy-Based Feedback Control
- Control Lyapunov Functions
- Hamilton-Jacobi-Bellman Equation
- Optimal Nonlinear Feedback Control
- Stability Margins of Nonlinear Regulators
- Nonlinear Disturbance Rejection Control
- Hamilton-Jacobi-Isaacs Equation
- Feedback Linearization, Zero Dynamics, and Minimum Phase Systems
- Backstepping Control
- Adaptive Control

**Course Objective:** To provide students with an advanced treatment of nonlinear dynamical systems and control as applied to aerospace systems.

**Office Hours:** M 3:30-4:30 pm.

Prerequisites:	1)	A course in classical control theory.
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- 2) A course in linear systems, state space models and matrix theory.
- 3) A willingness to work hard.

# **Computers:** Several assignments will require computations using MATLAB and the Control System Toolbox.

Course Structure:

- Homework/Projects 50% of grade
- Midterm Exam 20% of grade
- Final Exam 30% of grade

#### Homework/Project Requirements:

- Restate each problem before beginning to solve it.
- Write on only one side of each sheet of paper.
- Start each new problem on a new sheet of paper.
- Staple sheets together.
- Hand in *original*; keep a copy for yourself.
- "Neatness counts for points."

**Textbook:** W. M. Haddad and V. Chellaboina, *Nonlinear Dynamical Systems and Control: A Lyapunov-Based Approach,* Princeton University Press, 2008.

An updated list of errata and addenda to the book can be found under "Textbooks and Monographs" at: <u>http://haddad.gatech.edu</u>.

#### Additional Nonlinear Systems and Nonlinear Control Books

#### Major Texts:

H. K. Khalil, *Nonlinear Systems*, Third Edition, Prentice Hall, 2002.

M. Vidyasagar, Nonlinear Systems Analysis, Second Edition, Prentice Hall, 1993.

S. Sastry, Nonlinear Systems: Analysis, Stability, and Control, Springer, 1999.

There are numerous texts on ODEs. One is

J. K. Hale, Ordinary Differential Equations, Wiley-Interscience, 1969.

ODEs with discontinuous dynamics are considered in

A. F. Filippov, Differential Equations with Discontinuous Righthand Sides, Kluwer, 1988.

#### Some books devoted to stability theory:

W. Hahn, Theory and Application of Lyapunov's Direct Method, Prentice Hall, 1963.

K. S. Narendra and J. H. Taylor, *Frequency Domain Criteria for Absolute Stability*, Academic Press, 1973.

C. A. Desoer and M. Vidyasagar, *Feedback Systems: Input-Output Properties*, Academic Press, 1975.

P. Habets, N. Rouche, and M. Laloy, *Stability Theory by Lyapunov's Direct Method*, Springer, 1977.

V. I. Vorotnikov, Partial Stability and Control, Birkhauser, 1998.

#### Some more specialized texts:

A. Gelb and W. van der Velde, *Multiple Input Describing Functions and Nonlinear Systems Design*, McGraw Hill, 1968.

D. Atherton, Nonlinear Control Engineering, Van Nostrand Reinhold, 1975.

W. J. Rugh, *Nonlinear System Theory: The Volterra/Wiener Approach*, Johns Hopkins University Press, 1981.

E. P. Ryan, *Optimal Relay and Saturating Control System Synthesis*, Peter Peregrinus, 1982.

Y. Z. Tsypkin, *Relay Control Systems*, Cambridge University Press, 1984.

S. P. Banks, Mathematical Theories of Nonlinear Systems, Prentice Hall, 1988.

A. Isidori, Nonlinear Control Systems, 1989.

H. Nijmeijer and A. van der Schaft, Nonlinear Dynamical Control Systems, Springer, 1990.

J. B. Roberts and P.D. Spanos, *Random Vibration and Statistical Linearization*, Wiley, 1990.

J. J. E. Slotine and W. Li, Applied Nonlinear Control, Prentice Hall, 1991.

W. R. Kolk and R. A. Lerman, *Nonlinear System Dynamics*, Van Nostrand Reinhold, 1992.

R. M. Murray, Z. Li, and S. S. Sastry, *A Mathematical Introduction to Robotic Manipulation*, CRC, 1994.

R. Marino and P. Tomei, Nonlinear Control Design, Prentice Hall, 1995.

M. Krstic, I. Kanellakopoulos, and P. Kokotovic, *Nonlinear and Adaptive Control Design*, Wiley, 1995.

V. Jurdjevic, Geometric Control Theory, Cambridge University Press, 1997.

Z. Qu, Robust Control of Nonlinear Uncertain Systems, Wiley, 1998.

A. Isidori, Nonlinear Control Systems II, Springer, 1999.